

Write your name here	
Surname	Other names
<b>Pearson Edexcel</b> <b>Level 3 GCE</b>	<div style="display: flex; justify-content: space-between;"> <div style="text-align: center;">           Centre Number  <div style="border: 1px solid black; width: 40px; height: 20px; margin: 2px;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; margin: 2px;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; margin: 2px;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; margin: 2px;"></div> </div> <div style="text-align: center;">           Candidate Number  <div style="border: 1px solid black; width: 40px; height: 20px; margin: 2px;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; margin: 2px;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; margin: 2px;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; margin: 2px;"></div> </div> </div>
<h1 style="margin: 0;">Further Mathematics</h1> <p style="margin: 5px 0;"><b>Advanced Subsidiary</b></p> <p style="margin: 5px 0;"><b>Further Mathematics options</b></p> <p style="margin: 5px 0;"><b>25: Further Mechanics 1</b></p> <p style="margin: 5px 0;"><b>(Part of options C, E, H and J)</b></p>	
Thursday 17 May 2018 – Afternoon	Paper Reference <b>8FM0-25</b>
<b>You must have:</b> Mathematical Formulae and Statistical Tables, calculator	Total Marks <div style="border: 1px solid black; width: 60px; height: 40px; margin: 0 auto;"></div>

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.  
Answers without working may not gain full credit.
- Answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- The total mark for this part of the examination is 40. There are 4 questions.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

**P60206A**

©2018 Pearson Education Ltd.

1/1/1/



Whenever a numerical value of  $g$  is required, take  $g = 9.8 \text{ m s}^{-2}$  and give your answer to either 2 significant figures or 3 significant figures.

**Answer ALL questions. Write your answers in the spaces provided.**

1. A small ball of mass  $0.3 \text{ kg}$  is released from rest from a point  $3.6 \text{ m}$  above horizontal ground. The ball falls freely under gravity, hits the ground and rebounds vertically upwards.

In the first impact with the ground, the ball receives an impulse of magnitude  $4.2 \text{ N s}$ . The ball is modelled as a particle.

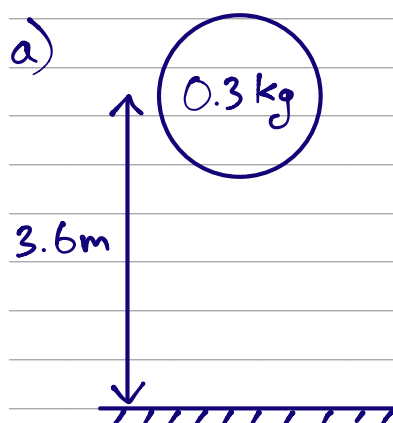
- (a) Find the speed of the ball immediately after it first hits the ground.

(5)

- (b) Find the kinetic energy lost by the ball as a result of the impact with the ground.

(3)

a)



To find speed of ball just before hitting the ground ( $v$ ) ( $\downarrow$  is +ve)

$$s = 3.6$$

$$u = 0$$

$$v = ?$$

$$a = 9.8$$

$$t =$$

$$v^2 = u^2 + 2as$$

$$v^2 = 0^2 + 2 \times 9.8 \times 3.6$$

$$v = \sqrt{70.56}$$

$$= 8.4 \text{ m s}^{-1}$$

To find speed of ball just after hitting the ground ( $w$ )

$$\text{Change in momentum} = I = mw - mv \quad (\uparrow \text{ is +ve})$$

$$4.2 = 0.3w - 0.3 \times (-8.4)$$

$$w = \frac{1.68}{0.3} = \underline{\underline{5.6 \text{ m s}^{-1}}}$$

b) KE lost during impact =  $\frac{1}{2}mv^2 - \frac{1}{2}mw^2$

$$= \frac{1}{2} \times 0.3 (8.4^2 - 5.6^2)$$

$$= \underline{\underline{5.88 \text{ J}}}$$



Question 1 continued

(Total for Question 1 is 8 marks)



P 6 0 2 0 6 A 0 3 1 6

2.

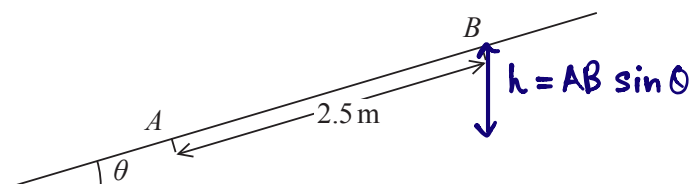


Figure 1

Figure 1 shows a ramp inclined at an angle  $\theta$  to the horizontal, where  $\sin \theta = \frac{2}{7}$

A parcel of mass 4 kg is projected, with speed  $5 \text{ m s}^{-1}$ , from a point  $A$  on the ramp. The parcel moves up a line of greatest slope of the ramp and first comes to instantaneous rest at the point  $B$ , where  $AB = 2.5 \text{ m}$ . The parcel is modelled as a particle.

The total resistance to the motion of the parcel from non-gravitational forces is modelled as a constant force of magnitude  $R$  newtons.

(a) Use the work-energy principle to show that  $R = 8.8$  (4)

After coming to instantaneous rest at  $B$ , the parcel slides back down the ramp. The total resistance to the motion of the particle is modelled as a constant force of magnitude 8.8 N.

(b) Find the speed of the parcel at the instant it returns to  $A$ . (3)

(c) Suggest two improvements that could be made to the model. (2)

a) Using the Work - Energy Principle,

$$\text{Initial KE} = \text{Final GPE} + \text{Work done by non-grav. forces}$$

$$\frac{1}{2}mv^2 = mg \times AB \sin \theta + R \times AB$$

$$\frac{1}{2} \times 4 \times 5^2 = 4 \times 9.8 \times 2.5 \times \frac{2}{7} + 2.5R$$

$$2.5R = 22$$

$$R = 8.8$$

b) Using the Work - Energy Principle for parcel sliding down

$$\text{GPE at B} = \text{KE at A} + \text{Work done by non-grav. forces}$$



Question 2 continued

$$mg \times AB \sin \theta = \frac{1}{2}mv^2 + 8.8 \times AB$$

$$4 \times 9.8 \times 2.5 \times \frac{2}{7} = \frac{1}{2} \times 4 \times v^2 + 8.8 \times 2.5$$

$$2v^2 = 6$$

$$v = \sqrt{3}$$

$$v \approx \underline{\underline{1.7 \text{ ms}^{-1}}} \text{ (To 2 s.f.)}$$

c) A variable resistance force can be used

A drag force (air resistance) proportional to the parcel's speed can be included



Question 2 continued

Lined area for writing the answer to Question 2.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 2 continued

Lined area for writing the answer to Question 2.

(Total for Question 2 is 9 marks)



3. A van of mass 750 kg is moving along a straight horizontal road. At the instant when the van is moving at  $v \text{ ms}^{-1}$ , the resistance to the motion of the van is modelled as a force of magnitude  $\lambda v \text{ N}$ , where  $\lambda$  is a constant.

The engine of the van is working at a constant rate of 18 kW.

At the instant when  $v = 15$ , the acceleration of the van is  $0.6 \text{ ms}^{-2}$

- (a) Show that  $\lambda = 50$

(4)

The van now moves up a straight road inclined at an angle to the horizontal, where

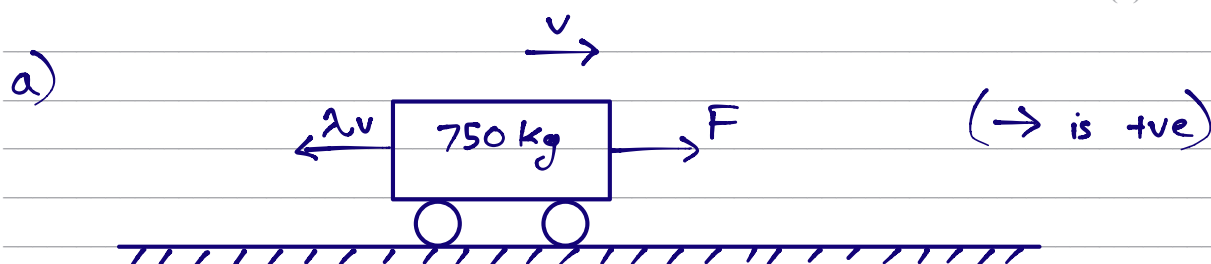
$$\sin \alpha = \frac{1}{15}$$

At the instant when the van is moving at  $v \text{ ms}^{-1}$ , the resistance to the motion of the van from non-gravitational forces is modelled as a force of magnitude  $50v \text{ N}$ .

When the engine of the van is working at a constant rate of 12 kW, the van is moving at a constant speed  $V \text{ ms}^{-1}$

- (b) Find the value of  $V$ .

(5)



Let  $F$  be the forward force on the van generated by the engine (of Power  $P$ )

$$P = Fv$$

$$F = \frac{P}{v}$$

Using Newton's 2<sup>nd</sup> Law:

$$F_{\text{net}} = ma$$

$$\frac{P}{v} - \lambda v = ma$$

When  $v = 15$ ,  $a = 0.6$

$$\frac{18000}{15} - 15\lambda = 750 \times 0.6$$

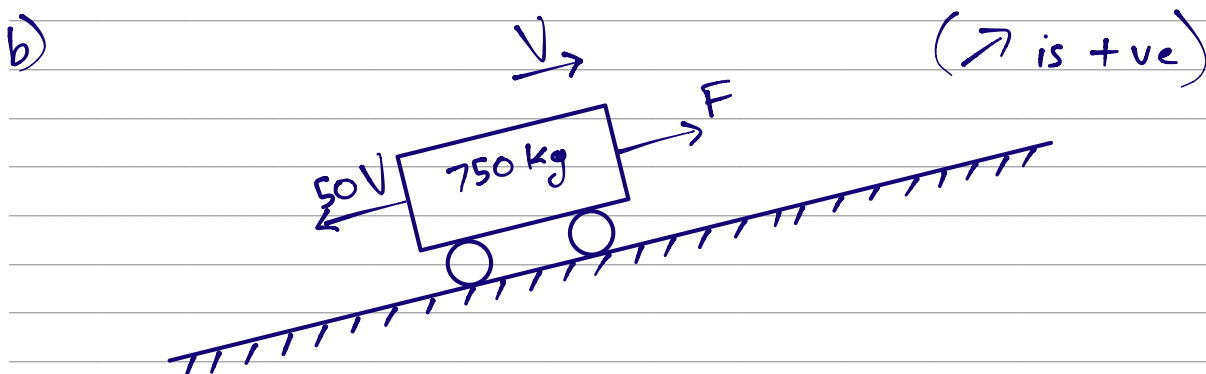




Question 3 continued

$$1200 - 15\lambda = 450$$

$$\lambda = \underline{\underline{50}}$$



Using Newton's 2<sup>nd</sup> Law, resolving up the ramp

$$F - 50V - mg \sin \alpha = ma$$

$$a = 0 \text{ (Constant speed)}$$

$$\frac{12000}{V} - 50V - 750 \times 9.8 \times \frac{1}{15} = 0$$

$$50V^2 + 490V - 12000 = 0$$

$$5V^2 + 49V - 1200 = 0$$

$$V = \frac{-49 \pm \sqrt{49^2 + 4 \times 5 \times 1200}}{2 \times 5}$$

$$= 11.34838... , -21.14838...$$

Since van is going up hill, take positive root  
 $\Rightarrow V = \underline{\underline{11.3}}$



Question 3 continued

Lined area for writing the answer to Question 3.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 3 continued

(Total for Question 3 is 9 marks)



P 6 0 2 0 6 A 0 1 1 1 6

4. A particle  $P$  of mass  $3m$  is moving in a straight line on a smooth horizontal floor. A particle  $Q$  of mass  $5m$  is moving in the opposite direction to  $P$  along the same straight line.

The particles collide directly.

Immediately before the collision, the speed of  $P$  is  $2u$  and the speed of  $Q$  is  $u$ .

The coefficient of restitution between  $P$  and  $Q$  is  $e$ .

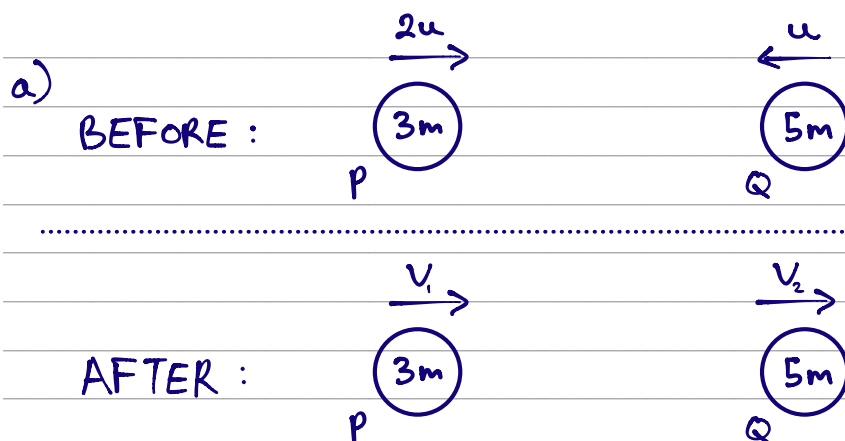
- (a) Show that the speed of  $Q$  immediately after the collision is  $\frac{u}{8}(9e + 1)$  (6)

- (b) Find the range of values of  $e$  for which the direction of motion of  $P$  is not changed as a result of the collision. (2)

When  $P$  and  $Q$  collide they are at a distance  $d$  from a smooth fixed vertical wall, which is perpendicular to their direction of motion. After the collision with  $P$ , particle  $Q$  collides directly with the wall and rebounds so that there is a second collision between  $P$  and  $Q$ . This second collision takes place at a distance  $x$  from the wall.

Given that  $e = \frac{1}{18}$  and the coefficient of restitution between  $Q$  and the wall is  $\frac{1}{3}$

- (c) find  $x$  in terms of  $d$ . (6)



Using the conservation of linear momentum ( $\rightarrow$  is +ve),

$$3mv_1 + 5mv_2 = 6mu - 5mu$$

$$3v_1 + 5v_2 = u \longrightarrow \textcircled{1}$$

Using Newton's Law of restitution,

$$e = \frac{v_2 - v_1}{2u + u} \Rightarrow v_2 - v_1 = 3eu \longrightarrow \textcircled{2}$$



Question 4 continued

To solve this system of linear equations,

$$\textcircled{1} + 3 \times \textcircled{2}: \quad 5v_2 + 3v_2 = u + 9eu$$

$$v_2 = \frac{u}{8} (9e + 1)$$

= Speed of Q just after collision

$$\begin{aligned} \text{b) Speed of P just after collision} &= v_1 \\ &= v_2 - 3eu \quad [\text{From } \textcircled{2}] \\ &= \frac{9}{8}eu + \frac{u}{8} - 3eu \\ &= \frac{u}{8} (1 - 15e) \end{aligned}$$

If direction of P is unchanged,

$$\begin{aligned} v_1 &> 0 \\ \frac{u}{8} (1 - 15e) &> 0 \end{aligned}$$

Since  $u \neq 0$  (or else the collision would not have happened)

$$\begin{aligned} 1 - 15e &> 0 \\ 15e &< 1 \\ e &< \frac{1}{15} \end{aligned}$$

$$\therefore 0 \leq e < \frac{1}{15}$$

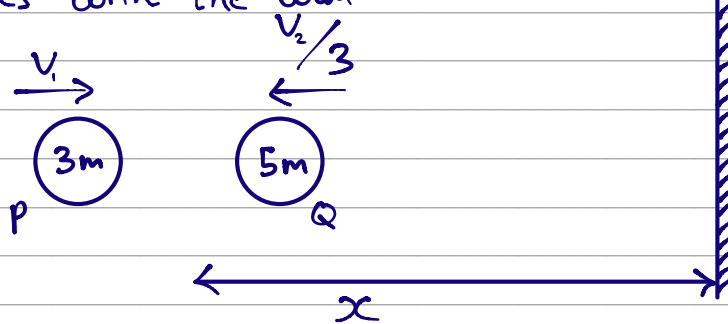


Question 4 continued

Just after 1<sup>st</sup> collision:



After Q collides with the wall:



In the time taken for Q to travel  $d+x$ , P travels  $d-x$

$$\text{Time elapsed for Q} = \text{Time elapsed for P}$$

$$\frac{d}{v_2} + \frac{x}{v_2/3} = \frac{d-x}{v_1}$$

$$\frac{d+3x}{\frac{4}{8}(9e+1)} = \frac{d-x}{\frac{4}{8}(1-15e)}$$

$$\text{Since } e = \frac{1}{18},$$

$$\frac{d+3x}{(\frac{1}{2}+1)} = \frac{d-x}{(1-\frac{15}{18})}$$

$$\frac{d+3x}{3/2} = \frac{d-x}{3/18}$$



Question 4 continued

$$2d + 6x = 18d - 18x$$

$$24x = 16d$$

$$x = \frac{2}{3}d$$



Question 4 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 4 is 14 marks)

TOTAL FOR FURTHER MECHANICS 1 IS 40 MARKS

